# 4

# **CHAPTER SUMMARY**

Big Idea 🚺

# For Your Notebook

## **Classifying Triangles by Sides and Angles**

**BIG IDEAS** 

	Equilateral	Isoso	celes	Scalene
Sides		XX		
	3 congruent side	congruent sides 2 or 3 congruent sides		No congruent sides
5:	Acute	Equiangular	Right	Obtuse
Angles		$\triangle$		
	3 angles < 90°	3 angles = 60°	1 angle = 90	0° 1 angle > 90°

# Big Idea 🙆

### **Proving That Triangles Are Congruent**

SSS	All three sides are congruent.	$\triangle ABC \cong \triangle DEF$	A = C D = F
SAS	Two sides and the included angle are congruent.	$\triangle ABC \cong \triangle DEF$	A = C  D = F
HL	The hypotenuse and one of the legs are congruent. (Right triangles only)	$\triangle ABC \cong \triangle DEF$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
ASA	Two angles and the included side are congruent.	$\triangle ABC \cong \triangle DEF$	A C D F
AAS	Two angles and a (non-included) side are congruent.	$\triangle ABC \cong \triangle DEF$	A C D F

# Big Idea 🔞

## **Using Coordinate Geometry to Investigate Triangle Relationships**

You can use the Distance and Midpoint Formulas to apply postulates and theorems to triangles in the coordinate plane.

# 4

# **CHAPTER REVIEW**

#### @HomeTutor

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- Multi-Language Glossary
- Vocabulary practice

## REVIEW KEY VOCABULARY

For a list of postulates and theorems, see pp. 926-931.

- triangle, p. 217 scalene, isosceles, equilateral, acute, right, obtuse, equiangular
- interior angles, p. 218
- exterior angles, p. 218
- corollary to a theorem, p. 220
- congruent figures, p. 225
- corresponding parts, p. 225
- right triangle, p. 241 legs, hypotenuse
- flow proof, p. 250
- isosceles triangle, p. 264 legs, vertex angle, base, base angles
- transformation, p. 272
- image, p. 272
- congruence transformation, p. 272 translation, reflection, rotation

#### **VOCABULARY EXERCISES**

- 1. Copy and complete: A triangle with three congruent angles is called \_?\_.
- **2. WRITING** *Compare* vertex angles and base angles.
- 3. WRITING Describe the difference between isosceles and scalene triangles.
- **4.** Sketch an acute scalene triangle. Label its interior angles 1, 2, and 3. Then draw and shade its exterior angles.
- **5.** If  $\triangle PQR \cong \triangle LMN$ , which angles are corresponding angles? Which sides are corresponding sides?

## REVIEW EXAMPLES AND EXERCISES

Use the review examples and exercises below to check your understanding of the concepts you have learned in each lesson of Chapter 4.

## 4.1 Apply Triangle Sum Properties

рр. 217–224

#### **EXAMPLE**

Find the measure of the exterior angle shown.

Use the Exterior Angle Theorem to write and solve an equation to find the value of *x*.



$$(2x - 20)^{\circ} = 60^{\circ} + x^{\circ}$$
 Apply the Exterior Angle Theorem.

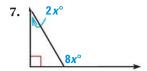
$$x = 80$$
 Solve for x.

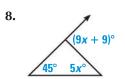
The measure of the exterior angle is  $(2 \cdot 80 - 20)^{\circ}$ , or  $140^{\circ}$ .

#### **EXERCISES**

on p. 219 for Exs. 6–8 Find the measure of the exterior angle shown.









# 4.2 Apply Congruence and Triangles

pp. 225-231

#### EXAMPLE

#### Use the Third Angles Theorem to find $m \angle X$ .

In the diagram,  $\angle A \cong \angle Z$  and  $\angle C \cong \angle Y$ . By the Third Angles Theorem,  $\angle B \cong \angle X$ . Then by the Triangle Sum Theorem,  $m\angle B = 180^{\circ} - 65^{\circ} - 51^{\circ} = 64^{\circ}$ .

So,  $m \angle X = m \angle B = 64^{\circ}$  by the definition of congruent angles.





# **EXERCISES EXAMPLES**In the diagra

**2 and 4** on pp. 226–227

for Exs. 9-14

EXAMPLE 1

for Exs. 15-16

on p. 234

In the diagram,  $\triangle ABC \cong \triangle VTU$ . Find the indicated measure.

11.  $m \angle T$ 

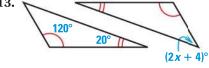
12. 
$$m \angle V$$



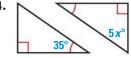


Find the value of x.

13.



14.



# **4.3** Prove Triangles Congruent by SSS

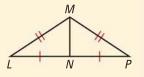
рр. 234–239

#### EXAMPLE

Prove that  $\triangle LMN \cong \triangle PMN$ .

The marks on the diagram show that  $\overline{LM} \cong \overline{PM}$  and  $\overline{LN} \cong \overline{PN}$ . By the Reflexive Property,  $\overline{MN} \cong \overline{MN}$ .

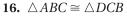
So, by the SSS Congruence Postulate,  $\triangle LMN \cong \triangle PMN$ .

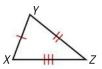


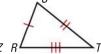
#### **EXERCISES**

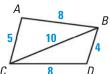
Decide whether the congruence statement is true. Explain your reasoning.

**15.** 
$$\triangle XYZ \cong \triangle RST$$









# 4

# **CHAPTER REVIEW**

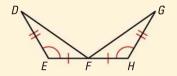
# 4.4 Prove Triangles Congruent by SAS and HL

рр. 240-246

#### EXAMPLE

Prove that  $\triangle DEF \cong \triangle GHF$ .

From the diagram,  $\overline{DE} \cong \overline{GH}$ ,  $\angle E \cong \angle H$ , and  $\overline{EF} \cong \overline{HF}$ . By the SAS Congruence Postulate,  $\triangle DEF \cong \triangle GHF$ .



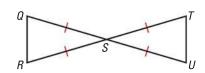
#### EXAMPLES 1 and 3

on pp. 240, 242 for Exs. 17–18

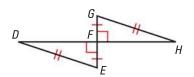
#### **EXERCISES**

Decide whether the congruence statement is true. Explain your reasoning.

**17.** 
$$\triangle QRS \cong \triangle TUS$$



**18.** 
$$\triangle DEF \cong \triangle GHF$$



# 4.5 Prove Triangles Congruent by ASA and AAS

рр. 249–255

#### EXAMPLE

Prove that  $\triangle DAC \cong \triangle BCA$ .

By the Reflexive Property,  $\overline{AC} \cong \overline{AC}$ . Because  $\overline{AD} \parallel \overline{BC}$  and  $\overline{AB} \parallel \overline{DC}$ ,  $\angle DAC \cong \angle BCA$  and  $\angle DCA \cong \angle BAC$  by the Alternate Interior Angles Theorem. So, by the ASA Congruence Postulate,  $\triangle ADC \cong \triangle ABC$ .

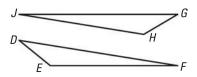


#### **EXERCISES**

State the third congruence that is needed to prove that  $\triangle DEF \cong \triangle GHJ$  using the given postulate or theorem.

#### EXAMPLES 1 and 2 on p. 250 for Exs. 19–20

- 19. **GIVEN**  $\triangleright \overline{DE} \cong \overline{GH}$ ,  $\angle D \cong \angle G$ , ?  $\cong$  ? Use the AAS Congruence Theorem.
- **20. GIVEN**  $\triangleright \overline{DF} \cong \overline{GJ}, \angle F \cong \angle J, \underline{?} \cong \underline{?}$  Use the ASA Congruence Postulate.



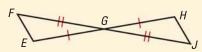
# **4.6** Use Congruent Triangles

pp. 256-263

#### EXAMPLE

GIVEN 
$$\blacktriangleright \overline{FG} \cong \overline{JG}, \overline{EG} \cong \overline{HG}$$

**PROVE** 
$$\triangleright \overline{EF} \cong \overline{HI}$$



You are given that  $\overline{FG} \cong \overline{JG}$  and  $\overline{EG} \cong \overline{HG}$ . By the Vertical Angles Theorem,  $\angle FGE \cong \angle JGH$ . So,  $\triangle FGE \cong \triangle JGH$  by the SAS Congruence Postulate. Corres. parts of  $\cong \triangle$  are  $\cong$ , so  $\overline{EF} \cong \overline{HJ}$ .



#### **EXAMPLE 3**

on p. 257 for Exs. 21–23

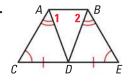
EXAMPLE 3

on p. 266 for Exs. 24–26

#### **EXERCISES**

Write a plan for proving that  $\angle 1 \cong \angle 2$ .

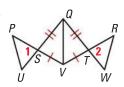
21.



22.



23.



#### 4.7 **Use Isosceles and Equilateral Triangles**

pp. 264-270

#### EXAMPLE

 $\triangle$  *QRS* is isosceles. Name two congruent angles.

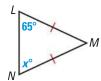
 $\overline{QR} \cong \overline{QS}$ , so by the Base Angles Theorem,  $\angle R \cong \angle S$ .



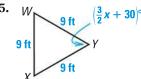
#### **EXERCISES**

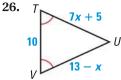
Find the value of x.

24.



**25.** 





#### 4.8 **Perform Congruence Transformations**

pp. 272-279

#### EXAMPLE

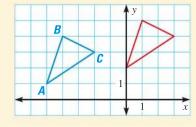
Triangle *ABC* has vertices A(-5, 1), B(-4, 4), and C(-2, 3). Sketch  $\triangle ABC$ and its image after the translation  $(x, y) \rightarrow (x + 5, y + 1)$ .

$$(x, y) \to (x + 5, y + 1)$$

$$A(-5, 1) \rightarrow (0, 2)$$

$$B(-4,4) \to (1,5)$$

$$C(-2,3) \to (3,4)$$



### **EXAMPLES**

2 and 3

on pp. 273-274

for Exs. 27-29

#### **EXERCISES**

Triangle QRS has vertices Q(2, -1), R(5, -2), and S(2, -3). Sketch  $\triangle QRS$ and its image after the transformation.

**27.** 
$$(x, y) \rightarrow (x - 1, y + 5)$$

**28.** 
$$(x, y) \to (x, -y)$$

**29.** 
$$(x, y) \to (-x, -y)$$